

Explain why each term is rational or irrational number.

1. $\sqrt{8} + 7$

irrational
it cannot be written as a fraction (ratio)

2. $(\sqrt{5})^2 = \sqrt{5} \cdot \sqrt{5} = 5$

rational: it can be written as a ratio

3. $0.\bar{2}$

rational: it has a repeating pattern

True or False (explain your reasoning).

4. The sum of two irrational numbers is always irrational.

False: Any number + its opposite = 0, which is a rational #.

ex. $\sqrt{5} + -\sqrt{5} = 0$; $\pi + -\pi = 0$

5. The product of a rational and an irrational is never rational.

False: Any number multiplied by 0 is 0, a rational #.
However, the product of a non-zero rational # and an irrational IS always irrational.

Add or Subtract:

6. $(5x^2 - 8x - 6) + (7x^2 - 9x - 3)$

$$5x^2 - 8x - 6 + 7x^2 - 9x - 3$$

$$12x^2 - 17x - 9$$

7. $(3x^2 + 5x - 9) - (6x^2 + 5x - 11)$

$$3x^2 + 5x - 9 - 6x^2 - 5x + 11$$

$$-3x^2 + 2$$

Multiply:

8. $7y^2(9y^3 - 8y + 4y^2)$

$$63y^5 - 56y^3 + 28y^4$$

9. $(x - 4)^2$

$$x^2 - 8x + 16$$

10. $(-2x + 1)(3x - 7)$

$$= -6x^2 + 14x + 3x - 7$$

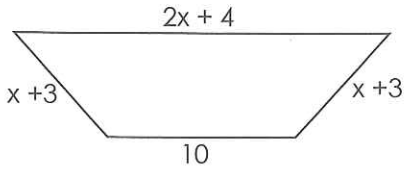
$$= -6x^2 + 17x - 7$$

11. $(x + 4)(6x^2 - 3x - 7)$

$$6x^3 - 3x^2 - 7x + 24x^2 - 12x - 28$$

$$6x^3 + 21x^2 - 19x - 28$$

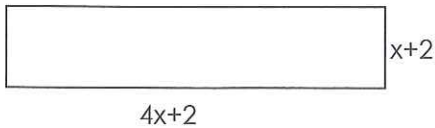
12. Give the perimeter of the deck shown below.



$$2x+4 + x+3 + 10 + x+3 = 4x+20$$

13. Find the area of the figures

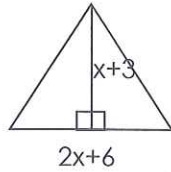
a)



$$A = lw$$

$$(x+2)(4x+2) = 4x^2 + 2x + 8x + 4 = 4x^2 + 10x + 4$$

b)

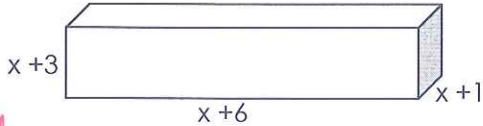


$$A = \frac{1}{2}bh$$

$$A = \frac{1}{2}(2x+6)(x+3) = \frac{1}{2}(2x^2 + 12x + 18)$$

$$A = x^2 + 6x + 9$$

14. Find the volume of the rectangular prism.



$$V = lwh$$

$$V = (x+3)(x+6)(x+1) = (x^2 + 9x + 18)(x+1) = x^3 + 9x^2 + 18x + x^2 + 9x + 18 = x^3 + 10x^2 + 27x + 18$$

Simplify each radical expression

15. $-3\sqrt{40} =$

$$-3\sqrt{4 \cdot 10} =$$

$$2 \cdot -3\sqrt{10} = -6\sqrt{10}$$

16. $11x\sqrt{120x^5y^6} =$

$$11x\sqrt{4 \cdot 30 \cdot x^4 \cdot x \cdot y^6} =$$

$$2 \cdot x^2 \cdot y^3 \cdot 11x\sqrt{30x} = 22x^3y^3\sqrt{30x}$$

17. $4ab\sqrt{250a^3b^2} =$

$$4ab\sqrt{25 \cdot 10 \cdot a^2 \cdot a \cdot b^2} =$$

$$5 \cdot a \cdot b \cdot 4ab\sqrt{10a} = 20a^2b^2\sqrt{10a}$$

Add/Subtract

18. $\sqrt{18} - 2\sqrt{27} + 3\sqrt{3} - 6\sqrt{8} =$

$$3\sqrt{2} - 6\sqrt{3} + 3\sqrt{3} - 12\sqrt{2} =$$

$$-9\sqrt{2} - 3\sqrt{3}$$

19. $4\sqrt{63} - 6\sqrt{28} + 9\sqrt{5} =$

$$12\sqrt{7} - 12\sqrt{7} + 9\sqrt{5} =$$

$$9\sqrt{5}$$

Multiply

20. $(3m\sqrt{8})^2 =$

$$(3m\sqrt{8})(3m\sqrt{8}) =$$

$$9m^2 \cdot 8 =$$

$$72m^2$$

21. $4\sqrt{10}(5\sqrt{2} - \sqrt{8}) =$

$$20\sqrt{20} - 4\sqrt{80} =$$

$$40\sqrt{5} - 16\sqrt{5} =$$

$$24\sqrt{5}$$

22. $(1 + \sqrt{2})(3 - \sqrt{2}) =$

$$3 - \sqrt{2} + 3\sqrt{2} - 2 =$$

$$1 + 2\sqrt{2}$$

Write an algebraic expression for each.

Write a verbal expression for the algebraic expression $7p - 11q$.

The difference between the product of 7 and p,
and the product of 11 and q.
one-third the square of a number

$$\frac{1}{3}x^2$$

Write an algebraic expression for the sum of five times r and s.

$$5r + s$$

Write an equation to represent "A number divided by six is 102."

and solve it.

$$\frac{n}{6} = 102 \quad \cancel{6} \frac{n}{\cancel{6}} = 102 \cdot 6 \quad \underline{n = 612}$$

Convert each using dimensional analysis.

26. A helicopter flying at a speed of 120 miles per hour. How fast is it traveling in feet per second?

$$\frac{120 \text{ miles}}{1 \text{ hr.}} \cdot \frac{5280 \text{ ft.}}{1 \text{ mile}} \cdot \frac{1 \text{ hr.}}{60 \text{ min.}} \cdot \frac{1 \text{ min.}}{60 \text{ sec.}} = \underline{176 \text{ ft./second}}$$

27. Bill Gates owns 3850 square kilometers of land. Convert this to square meters.

$$\frac{3850 \text{ km}^2}{1} \cdot \frac{1000 \text{ m}^2}{\text{km}^2} = \underline{3,850,000 \text{ square meters}}$$

28. How many liters of gasoline are needed to fill a 13.2-gallon tank? There are about 1.06 quarts per 1 liter and 4 quarts to 1 gallon.

$$\frac{13.2 \text{ gallons}}{1} \cdot \frac{4 \text{ qts.}}{\text{gallon}} \cdot \frac{1 \text{ liter}}{1.06 \text{ qts.}} = 12.45 \text{ liters}$$

29. Shane bikes 5 miles to the park in 30 minutes. What is his average speed in feet per second?

$$\frac{5 \text{ miles}}{30 \text{ min.}} \cdot \frac{5280 \text{ ft.}}{1 \text{ mile}} \cdot \frac{1 \text{ min.}}{60 \text{ sec.}} = \underline{14.67 \text{ ft./second}}$$